

Cesàro's 2nd sort of

→ C. sort of

$$\sum a_n$$

$$\lim_{n \rightarrow \infty} \frac{S_0 + S_1 + \dots + S_n}{n+1} = \Delta$$

$$\sum_{n=1}^{\infty} n = 1 + 2 + 3 + 4 + 5$$

$a_0 \quad a_1 \quad a_2$

$$S_0 = 1$$

$$S_1 = 1 + 2 = 3$$

$$S_2 = 1 + 2 + 3 = 6$$

$$S_3 = 1 + 2 + 3 + 4 = 10$$

⋮

$$S_n =$$

$$= \frac{(n+1)(n+2)}{2}$$

$$\frac{(3+1)(3+2)}{2} = 10$$

$$\lim_{n \rightarrow \infty} \frac{S_0 + S_1 + S_2 + \dots + S_n}{n+1} = \lim_{n \rightarrow \infty} \frac{1 + 3 + 6 + 10 + \dots + \frac{(n+1)(n+2)}{2}}{n+1}$$

$\underbrace{\hspace{10em}}_{*}$

$$= \infty$$

$$* \geq$$

$$\frac{\frac{(n+1)(n+2)}{2}}{n+1}$$

1 polcajt

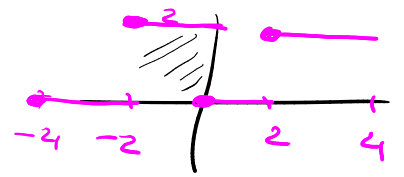
$$\lim_{n \rightarrow \infty} \frac{(n+1)(n+2)}{2(n+1)} = \infty$$

Fourier series

$$a_k = \frac{1}{L} \int_{-L}^L f(x) \cos\left(\frac{\pi k x}{L}\right) dx \quad k \in \mathbb{N}_0$$

$$b_k = \frac{1}{L} \int_{-L}^L f(x) \sin\left(\frac{\pi k x}{L}\right) dx \quad k \in \mathbb{N}$$

Def. $f(x) = \begin{cases} 0 & x \in [0, 2) \\ 2 & x \in [2, 4) \end{cases}$



$$2L = 4 \quad L = 2$$

$$a_0 = \frac{1}{2} \int_{-2}^2 f(x) dx = \frac{1}{2} \int_{-2}^0 0 dx + \frac{1}{2} \int_0^2 2 dx = \frac{1}{2} \cdot 2 \cdot 2 = 2$$

$$\begin{aligned} a_2 &= \frac{1}{2} \int_{-2}^2 f(x) \cos\left(\frac{\pi \cdot 2 x}{2}\right) dx = \frac{1}{2} \int_{-2}^0 0 \cos\left(\frac{\pi \cdot 2 x}{2}\right) dx + \frac{1}{2} \int_0^2 2 \cos\left(\frac{\pi \cdot 2 x}{2}\right) dx = \\ &= \left[\frac{2}{2\pi} \sin\left(\frac{\pi \cdot 2 x}{2}\right) \right]_0^2 = 0 - \frac{2}{2\pi} \sin\left(\frac{\pi \cdot 2 \cdot (-2)}{2}\right) = 0 \end{aligned}$$



$$\begin{aligned} b_2 &= \frac{1}{2} \int_{-2}^2 2 \sin\left(\frac{\pi \cdot 2 x}{2}\right) dx = \left[\frac{2}{2\pi} \left(-\cos\left(\frac{\pi \cdot 2 x}{2}\right) \right) \right]_{-2}^0 = \frac{-2}{2\pi} - \frac{-2}{2\pi} \cos(\pi) \\ &= \frac{-2}{2\pi} (1 - (-1)^2) \quad \begin{matrix} \text{scale} \\ \text{factor} \end{matrix} \end{aligned}$$

$$f(x) = \frac{2}{2} + \sum_{k=1}^{\infty} \frac{-2}{2\pi} (1 - (-1)^k) \sin \frac{kx\pi}{2}$$