

$$\sum_{n=1}^{\infty} (-1)^n \frac{n^2}{n! \cdot 2^n}$$

• $f(x) = \sum_{n=1}^{\infty} \frac{n^2}{n!} x^{n-1}$ $x \in (-\infty, \infty)$
 $x \rightarrow \frac{1}{2^{1/2}}$

$$F(x) = \sum_{n=1}^{\infty} \frac{n}{n!} x^n = x \sum_{n=1}^{\infty} \frac{n}{n!} x^{n-1} = x \cdot g(x)$$

$$G(x) = \sum_{n=1}^{\infty} \frac{x^n}{n!} = \underline{e^x - 1} \quad g = G' = e^x \therefore$$

$$1 + \frac{x^1}{1!} + \frac{x^2}{2!} + \dots$$

$$F(x) = x e^x$$

$$\boxed{f = f' = e^x + x e^x}$$

• Попробуем $\sum_{n=1}^{\infty} \frac{n^2}{n!} x^{n-1}$

$$a_n = \frac{(n+1)^2}{(n+1)!}$$

$$\cancel{\frac{1}{n!} x^n}$$

$$x^n = x^{n-1}$$

$$n = n-1$$

$$n+1 = n$$

$$R = \limsup_{n \rightarrow \infty} \sqrt[n]{\frac{(n+1)^2}{(n+1)!}}$$

$$= \frac{1}{\frac{n}{n} \cdot \frac{1}{n}} = \frac{1}{0} = \infty$$

Рассуждения не $x \in (-\infty, \infty)$

$$f(x) = \sum_{n=1}^{\infty} \frac{n^2}{n!} x^{n-1}$$

$$f(x) = e^x + x e^x$$

$$= \sum_{n=1}^{\infty} \frac{n^2}{n!} \left(\frac{-1}{2}\right)^{n-1}$$

$$-\frac{1}{2} \cdot f\left(\frac{-1}{2}\right) = \sum_{n=1}^{\infty} \frac{n^2}{n!} \left(\frac{-1}{2}\right)^{n-1}$$

$$L_2 = -\frac{1}{2} \left(e^{-1/2} + -\frac{1}{2} e^{-1/2} \right) =$$

$$= -\frac{1}{4} \frac{1}{\sqrt{e}}$$

Indy by $x = \frac{1}{2}$

$$\bullet \sum_{n=1}^{\infty} \frac{x^n}{n!} \left(-\frac{1}{2}\right)^{n-1} \quad x = \frac{1}{2}$$

$$d'f \rightarrow x \therefore$$

$$\bullet \lim_{x \rightarrow \frac{1}{2}^+} f(x) = \sum_{n=1}^{\infty} \frac{x^n}{n!} \left(-\frac{1}{2}\right)^{n-1}$$