

$$\sum | \underbrace{e^{\frac{1}{\sqrt{n}}} - \sin \frac{1}{\sqrt{n}} - 1}_{a_n} |$$

$$\underline{x_n = \frac{1}{\sqrt{n}}} \quad \frac{1}{\sqrt{n}} \rightarrow 0$$

$$f(x) = e^x - \sin x - 1$$

$$= \cancel{1} + \cancel{x} + \frac{x^2}{2} + o(x^2) - \left(\cancel{x} - \frac{x^3}{6} + o(x^4) \right) - \cancel{1}$$

$$= \frac{x^2}{2} + o(x^2) - \frac{x^3}{6} + o(x^4)$$

$$\approx \frac{x^2}{2} + o(x^2)$$

$$a_n \approx \frac{\left(\frac{1}{\sqrt{n}}\right)^2}{2} \quad \frac{1}{\sqrt{n}} = b_n \quad \text{LStk}$$

$$\lim_{n \rightarrow \infty} \frac{|a_n|}{b_n} = \lim_{n \rightarrow \infty} \frac{|e^{\frac{1}{\sqrt{n}}} - \sin \frac{1}{\sqrt{n}} - 1|}{\frac{1}{\sqrt{n}}} = \frac{1}{2}$$

Heine $x_n = \frac{1}{\sqrt{n}} \in (0, \infty)$

$$\lim_{x \rightarrow 0} \frac{|e^x - \sin x - 1|}{x^2} = \frac{1}{2}$$

$$\lim_{x \rightarrow 0} \frac{\frac{x^2}{2} + o(x^2)}{x^2} = \frac{1}{2} + 0$$

$$\sum b_n \text{ D} \Rightarrow \left[\sum |a_n| \text{ D} \right]$$

$$\lim_{n \rightarrow \infty} \frac{1}{n} \quad x_n = \frac{1}{n} \quad x_n \rightarrow 0$$

$$\lim_{x \rightarrow 0} (1+x)^{\frac{1}{x}} = e$$

$$1 + \underbrace{(x-1)}_{\frac{1}{n}} \cdot \frac{1}{x}$$

$$\ln(\sin x \cdot \frac{1}{x})$$

$$1 - \frac{x^2}{6} + O(x^3)$$

$$\lim_{x \rightarrow 0} \frac{O(x^4)}{x^4} = 0$$

$$\lim_{x \rightarrow 0} \frac{O(x^4)}{x^3 - x} \cdot \frac{x}{0} = 0 \quad \checkmark$$